

$$x dy - y dx = (xy)^{\frac{1}{2}} dx$$

(1)

$$x \frac{dy}{dx} - y = x^{\frac{1}{2}} y^{\frac{1}{2}}$$

$$y' - \frac{1}{x} y = x^{-\frac{1}{2}} y^{\frac{1}{2}}$$

$y' + p(x)y = y^n Q(x)$ (משוואה דיפרנציאלה מסוג Bernoulli $n \neq 1$ ו/או $n \neq 0$ במקרה זה) $\frac{y' + p(x)y}{y^n} = \frac{Q(x)}{y^{n-1}}$
 פתרון: $y^{1-n} = \left[C + (1-n) \int Q(x) e^{\int (1-n)p(x) dx} dx \right] e^{-\int (1-n)p(x) dx}$

$$n = \frac{1}{2} \Rightarrow 1 - n = \frac{1}{2}, \quad P(x) = -\frac{1}{x}, \quad Q(x) = x^{-\frac{1}{2}}$$

$$y^{1/2} = \left[C + \frac{1}{2} \int x^{-\frac{1}{2}} e^{\int -\frac{1}{2} \frac{1}{x} dx} dx \right] e^{\int \frac{1}{2} \frac{1}{x} dx}$$

$$y^{1/2} = \left[C + \frac{1}{2} \int x^{-\frac{1}{2}} e^{-\frac{1}{2} \ln x} dx \right] e^{\frac{1}{2} \ln x}$$

$$y^{1/2} = \left[C + \frac{1}{2} \int x^{-\frac{1}{2}} e^{\ln x^{-1/2}} dx \right] e^{\ln x^{1/2}}$$

$$y^{1/2} = \left[C + \frac{1}{2} \int x^{-\frac{1}{2}} x^{-\frac{1}{2}} dx \right] x^{\frac{1}{2}}$$

$$y^{1/2} = \left[C + \frac{1}{2} \int \frac{1}{x} dx \right] \sqrt{x}$$

$$y^{1/2} = \left[C + \frac{1}{2} \ln x \right] \sqrt{x}$$

$$y^{1/2} = [C + \ln \sqrt{x}] \sqrt{x}$$

$$y = x(C + \ln \sqrt{x})^2$$