

$$z_{(x,y)} = x\varphi_{(x+y)} + y\psi_{(x+y)} \leftarrow \mathbf{t = x + y}$$

$$z_{(x,y)} = x\varphi_{(t)} + y\psi_{(t)} \quad \frac{\partial \mathbf{t}}{\partial x} = \mathbf{1}$$

$$\frac{\partial z}{\partial x} = \left( 1 \cdot \varphi_{(t)} + x \cdot \frac{\partial \varphi_{(t)}}{\partial x} \right) + y \cdot \frac{\partial \psi_{(t)}}{\partial x}$$

ל轻松מת לבכם :

$$\varphi_{(t(x))} \Rightarrow \frac{\partial \varphi_{(t)}}{\partial x} = \frac{\partial \varphi_{(t)}}{\partial t} \cdot \frac{\partial \mathbf{t}}{\partial x} = \frac{\partial \varphi_{(t)}}{\partial t}$$

$$\psi_{(t(x))} \Rightarrow \frac{\partial \psi_{(t)}}{\partial x} = \frac{\partial \psi_{(t)}}{\partial t} \cdot \frac{\partial \mathbf{t}}{\partial x} = \frac{\partial \psi_{(t)}}{\partial t}$$

ולכן אפשר לרשום את אגף ימין כדלקמן :

$$\frac{\partial z}{\partial x} = \varphi_{(t)} + x \cdot \frac{\partial \varphi_{(t)}}{\partial t} + y \cdot \frac{\partial \psi_{(t)}}{\partial t}$$

$$\frac{\partial^2 z}{\partial x^2} = \frac{\partial \varphi_{(t)}}{\partial x} + \frac{\partial}{\partial x} \left( x \cdot \frac{\partial \varphi_{(t)}}{\partial t} \right) + \frac{\partial}{\partial x} \left( y \cdot \frac{\partial \psi_{(t)}}{\partial t} \right)$$

$$\frac{\partial^2 z}{\partial x^2} = \frac{\partial \varphi_{(t)}}{\partial t} + \left( 1 \cdot \frac{\partial \varphi_{(t)}}{\partial t} + x \cdot \frac{\partial}{\partial x} \frac{\partial \varphi_{(t)}}{\partial t} \right) + y \cdot \frac{\partial}{\partial x} \frac{\partial \psi_{(t)}}{\partial t}$$

$$\frac{\partial^2 z}{\partial x^2} = \varphi_t + \left( \varphi_t + x \cdot \frac{\partial}{\partial x} \varphi_t \right) + y \cdot \frac{\partial}{\partial x} \psi_t \quad \leftarrow \text{Note! do not confuse } f_{(t)} \text{ with } f_t$$

$$\frac{\partial^2 z}{\partial x^2} = 2\varphi_t + x \cdot \frac{\partial \varphi_t}{\partial t} + y \cdot \frac{\partial \psi_t}{\partial t} \quad \leftarrow \text{more compactly written}$$

ש לבחור תשובה אחת:

$$\frac{\partial^2 z}{\partial x^2} = \frac{\vartheta \varphi}{\vartheta t} + y \cdot \frac{\vartheta^2 \varphi}{\vartheta t^2} + x \cdot \frac{\vartheta^2 \psi}{\vartheta t^2} .a$$

$$\frac{\partial^2 z}{\partial x^2} = 2 \frac{\vartheta \varphi}{\vartheta t} + y \cdot \frac{\vartheta^2 \varphi}{\vartheta t^2} + x \cdot \frac{\vartheta^2 \psi}{\vartheta t^2} .b$$

$$\frac{\partial^2 z}{\partial x^2} = 2 \frac{\vartheta \varphi}{\vartheta t} + x \cdot \frac{\vartheta^2 \varphi}{\vartheta t^2} + y \cdot \frac{\vartheta^2 \psi}{\vartheta t^2} .c$$

$$\frac{\partial^2 z}{\partial x^2} = \frac{\vartheta \varphi}{\vartheta t} + \frac{\vartheta^2 \varphi}{\vartheta t^2} + (x+y) \frac{\vartheta^2 \psi}{\vartheta t^2} .d$$

שוב,轻松מת לבכם :

$$\varphi_{t(t(x))} \Rightarrow \frac{\partial \varphi_t}{\partial x} = \frac{\partial \varphi_t}{\partial t} \cdot \frac{\partial \mathbf{t}}{\partial x} = \frac{\partial \varphi_t}{\partial t}$$

$$\psi_{t(t(x))} \Rightarrow \frac{\partial \psi_t}{\partial x} = \frac{\partial \psi_t}{\partial t} \cdot \frac{\partial \mathbf{t}}{\partial x} = \frac{\partial \psi_t}{\partial t}$$

ולכן אפשר לרשום את אגף ימין כך :

$$\frac{\partial^2 z}{\partial x^2} = 2\varphi_t + x \cdot \frac{\partial \varphi_t}{\partial t} + y \cdot \frac{\partial \psi_t}{\partial t}$$

או בכתב אחר :

$$\frac{\partial^2 z}{\partial x^2} = 2 \frac{\partial \varphi}{\partial t} + x \cdot \frac{\partial^2 \varphi}{\partial t^2} + y \cdot \frac{\partial^2 \psi}{\partial t^2}$$

היו  $\psi(t)$  פונקציות גיארת ברכיפות פעמיות.  
נגדה:  $z(x,y) = x\varphi(x+y) + y\psi(x+y)$   
ערם של  $\frac{\vartheta^2 z}{\vartheta x^2}$  בנקודה מסוימת.  
תשובה: